

5. Given a set of premises, construct a proof using the rules of inference.

Premise 1: $(a \wedge b) \vee \neg a$

Premise 2: $b \rightarrow c$

Premise 3: $e \leftrightarrow c$

Prove that $a \rightarrow e$

① $(\neg a \vee a) \wedge (\neg a \vee b)$

Distributive Law applied to Premise 1

② $T \wedge (\neg a \vee b)$

Trivial tautology in ①

③ $(\neg a \vee b)$

Identity law applied to ②

④ $a \rightarrow b$

Definition of implication

⑤ $a \rightarrow c$

Hypothetical syllogism of ④ and Premise 2.

⑥ $(e \rightarrow c) \wedge (c \rightarrow e)$

Definition of \leftrightarrow

⑦ $c \rightarrow e$

Simplification of ⑥

⑧ $a \rightarrow e$

Hypothetical syllogism applied to ⑤ and ⑦.

Let $A = \{0, 3, 9\}$ and $B = \{-1, 1, 3, 6, 11\}$.

6. a. What is $A \cup B$?

$\{-1, 0, 1, 3, 6, 9, 11\}$

b. What is $A \cap B$?

$\{3\}$

c. Is $(A - B) \supseteq (B - A)$?

No.

d. Is $B \subseteq (B \cap A)$?

No.

