

Note that

$$n(T) = n(T_1) + n(T_2) + 1$$

and

$$h(T) = \max(h(T_1), h(T_2)) + 1$$

Proof:

$$n(T) = n(T_1) + n(T_2) + 1$$

$$\geq (2h(T_1) + 1) + (2h(T_2) + 1) + 1$$

by inductive assumption

$$= 2(h(T_1) + h(T_2)) + 3$$

$$\geq 2(\max(h(T_1), h(T_2))) + 3$$

~~by inductive assumption~~

$$= 2(\max(h(T_1), h(T_2)) + 1) + 1$$

$$= 2(h(T)) + 1$$

by def. of $h(T)$

Therefore,

$$n(T) \geq 2h(T) + 1$$