

Case A)  $(k+1) \bmod 3 = 0$

According to the non-recursive formula:

$$f(k+1) = 2^{\lfloor (k+1)/3 \rfloor}$$

According to the recursive formula:

$$f(k+1) = 2 f((k+1)-3)$$

$$= 2 f(k-2)$$

$$= 2 \left( 2^{\lfloor (k-2)/3 \rfloor} \right)$$

Justification:

According to the inductive assumption, the non-recursive and recursive formulas are equivalent for  $n \leq k$ . Thus, we can substitute the non-recursive function definition for  $f(k-2)$ .

Since we know that  $(k+1) \bmod 3 = 0$ ,

it must be true that  $((k+1)-3) \bmod 3 = 0$

and  $(k-2) \bmod 3 = 0$

Thus,  $f(k-2) = 2^{\lfloor (k-2)/3 \rfloor}$

$$= 2^{\lfloor (k-2)/3 \rfloor + 1}$$

$$= 2^{\lfloor (k-2+3)/3 \rfloor}$$

$$= 2^{\lfloor (k+1)/3 \rfloor}$$

Therefore, for case A the recursive and non-recursive formulas are equivalent.