

## CS 381 Solutions to Homework 10

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- b) Reflexive, symmetric, not antisymmetric, and transitive.
- d) Reflexive, symmetric, not antisymmetric, and not transitive.

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b)  $R_1$ ,

c)  $\emptyset$

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$\{ \langle 1, 1 \rangle, \langle 1, 2 \rangle, \langle 2, 1 \rangle, \langle 2, 2 \rangle \}$ .

For example  $\langle 1, 2 \rangle$  in  $R$  and  $\langle 2, 1 \rangle$  in  $S$  produce  $\langle 1, 1 \rangle$  in  $S \circ R$ , and  $\langle 1, 3 \rangle$  in  $R$  and  $\langle 3, 2 \rangle$  in  $S$  produce  $\langle 1, 2 \rangle$  in  $S \circ R$ .

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- b) Since  $R$  and  $S$  are reflexive, for an arbitrary  $x \in A$ ,  $(x, x) \in R$  and  $(x, x) \in S$ .  
Hence for an arbitrary  $x \in A$ ,  $(x, x) \in R \cap S$ . Hence  $R \cap S$  is reflexive.

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32.

#	Reflexive	Irreflexive	Symmetric	Antisymmetric	Transitive
26	Yes	No	No	No	No
27	No	No	Yes	No	No

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2.  $R$  is symmetric. Hence it is its own symmetric closure.

9. Symmetric closure of 5:  $\{ (a, b), (b, a), (a, c), (c, a), (b, d), (d, b), (c, d), (d, c) \}$

20 b)  $(a, b)$  in  $R^3$  means that there is a two-stop (three leg) airline flight from city  $a$  to city  $b$ .

24. Not necessarily. For example let  $R = \{ \langle a, b \rangle, \langle b, a \rangle \}$  on the set  $\{a, b\}$ . Then  $R^2 = \{ \langle a, a \rangle, \langle b, b \rangle \}$ , which is not irreflexive.